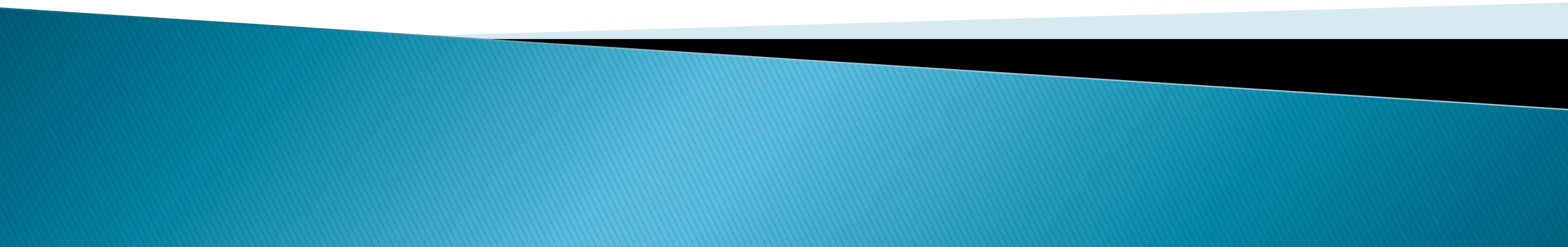


# Real Time Systems 2

## **Myopic Offline Scheduling Algorithm**

### Lecture 7



# Myopic Offline Scheduling algorithm

- ▶ **Myopic Offline Scheduling** (MOS) heuristic is an assignment/scheduling algorithm meant for non-preemptive tasks.
- ▶ This algorithm takes account not only of **processing needs** but also of any requirements that tasks may have for **additional resources**.
- ▶ For example, a task may need to have exclusive access to a block of memory or may need to have control over a printer.
- ▶ MOS is an **offline** algorithm in that we are given in advance the entire set of tasks, their arrival time, execution time and deadline

# Myopic Offline Scheduling algorithm

- ▶ MOS proceeds by building up a schedule tree.
- ▶ Each node in this tree represents an assignment and scheduling of a subset of tasks.
- ▶ The root of the schedule tree is an empty schedule.
- ▶ Each child of a node consists of the schedule of its parents node, extended by one task.
- ▶ A leaf of this tree consists of a schedule (feasible or infeasible) of the entire task set.

# Myopic Offline Scheduling algorithm

- ▶ The schedule tree for an  $nT$  task system consists of  $nT+1$  levels (including the root).
- ▶ Level  $i$  of the tree (counting the root as being of level 0) consists of nodes representing schedules including exactly  $i$  of tasks.
- ▶ Generating the complete tree is tantamount to an exclusive enumeration of all possible allocations.
- ▶ For any but the smallest systems, it is therefore not practical to generate the complete tree.
- ▶ Instead, we try to get to a feasible schedule as quickly as we can.

# Myopic Offline Scheduling algorithm

- ▶ The algorithm:
- ▶ We start at the root node, which is an empty schedule, that is, it corresponds to no task having been scheduled.
- ▶ We then proceed to build the tree from that point by developing nodes.
- ▶ A node is developed as follows:
- ▶ Given a node  $n$ , we try to extend the schedule represented by that node by one or more tasks.
- ▶ That is, we pick up one of the as-yet-unscheduled tasks and try to add it to the schedule represented by node  $n$ . The augmented schedule is a child node of  $n$ .

# Myopic Offline Scheduling algorithm

- ▶ There are two questions that must be answered:
- ▶ **First:** Which task do we pick for extending an incomplete schedule?
- ▶ **Second:** When do we decide that a node is not worth developing further and turn to another node?

# Myopic Offline Scheduling algorithm

- ▶ 1. The task that we chose to extend an incomplete schedule is one that minimize a heuristic function  $H$ .  $H$  may be any of the following functions:
  - ▶ Task execution time.
  - ▶ Deadline
  - ▶ Earliest start time.
  - ▶ Laxity. ( $D_i - e_i$ ).
  - ▶ Weighted sum of any of the above.



# Myopic Offline Scheduling algorithm

- ▶ 2. We only develop a node if it is strongly feasible.
- ▶ A node is strongly feasible if a feasible schedule can be generated by extending the current partial schedule with any one of the as-yet-unscheduled tasks.
- ▶ If a node is not strongly feasible, it means that none of its descendants that are leaves can represent a feasible schedule.
- ▶ If we encounter a node that is not strongly feasible, we backtrack.
- ▶ That is, we mark that node as hopeless, and then go back to its parent, resuming the schedule-building from that point.



# Myopic Offline Scheduling algorithm

- ▶ One difficulty with the MOS algorithm is that, if the number of tasks is very large, it can take a long time to check if a node is strongly feasible.
- ▶ In particular, at level  $l$ , we will need to check feasibility of extending the schedule by each of the  $nT - l$  as-yet-unscheduled tasks.
- ▶ As a result, the number of comparisons needed to generate one root-to-leaf path is:
  - ▶  $nT + (nT-1) + (nT-2) + \dots + 0 = (nT * (nT + 1)) / 2$

# Myopic Offline Scheduling algorithm

- ▶ To reduce the number of comparisons, we can replace the strongly feasibility check at each node by means of myopic procedure as follows:
- ▶ For each nonleaf level- $i$  node  $n$ , this procedure picks the first
- ▶  $\min \{k, nT-i\}$  as-yet-unscheduled tasks and checks to see if the schedule represented by  $n$  can be feasibly extended by each of these tasks.
- ▶ If not, we mark the node as hopeless and backtrack as before.
- ▶ Otherwise, we develop children for that node.

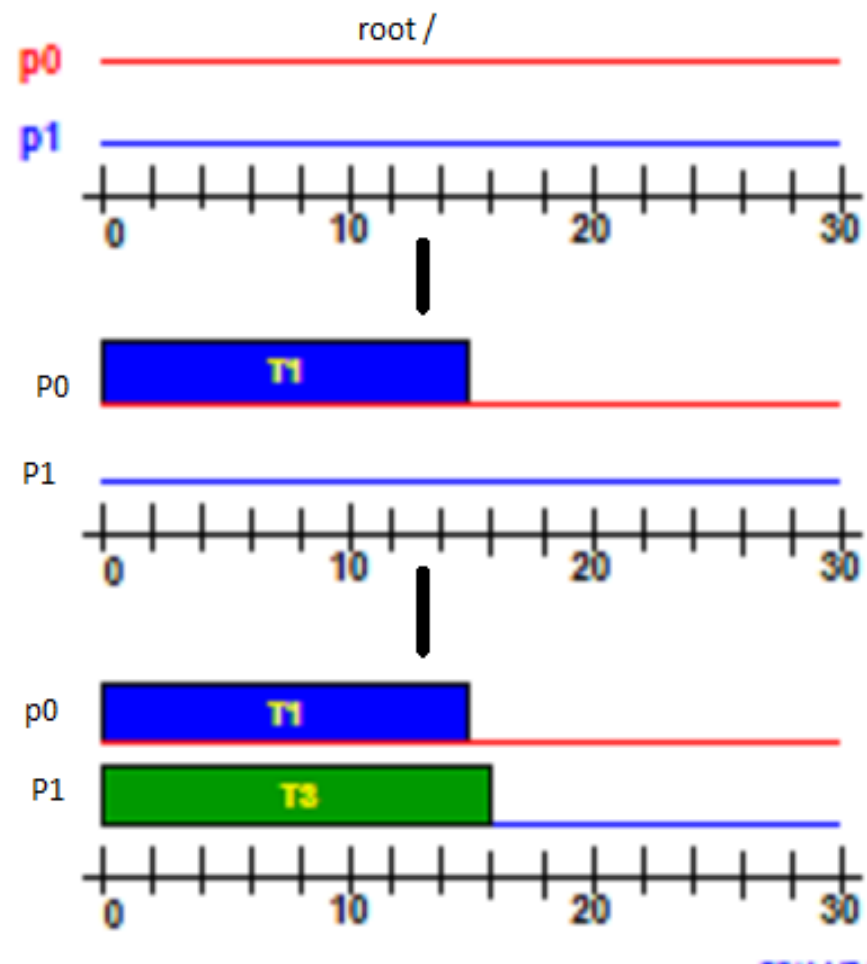
# Myopic Offline Scheduling algorithm

- ▶ **Example:** We have a five task set to be scheduled on two-processor system.
- ▶ The tasks are non-preemptive. The parameters of these tasks are as follows: There are no other resource requirements. Suppose we use  $H(i)=r_i$  . We set  $k=5$  for the myopic procedure.

	T1	T2	T3	T4	T5
$R_i$	0	10	0	15	0
$E_i$	15	5	16	9	10
$D_i$	15	20	18	25	50

# Myopic Offline Scheduling algorithm

- ▶ The root node is the empty schedule. There are three tasks with release time = 0. we pick T1 first. A level-1 node is generated.



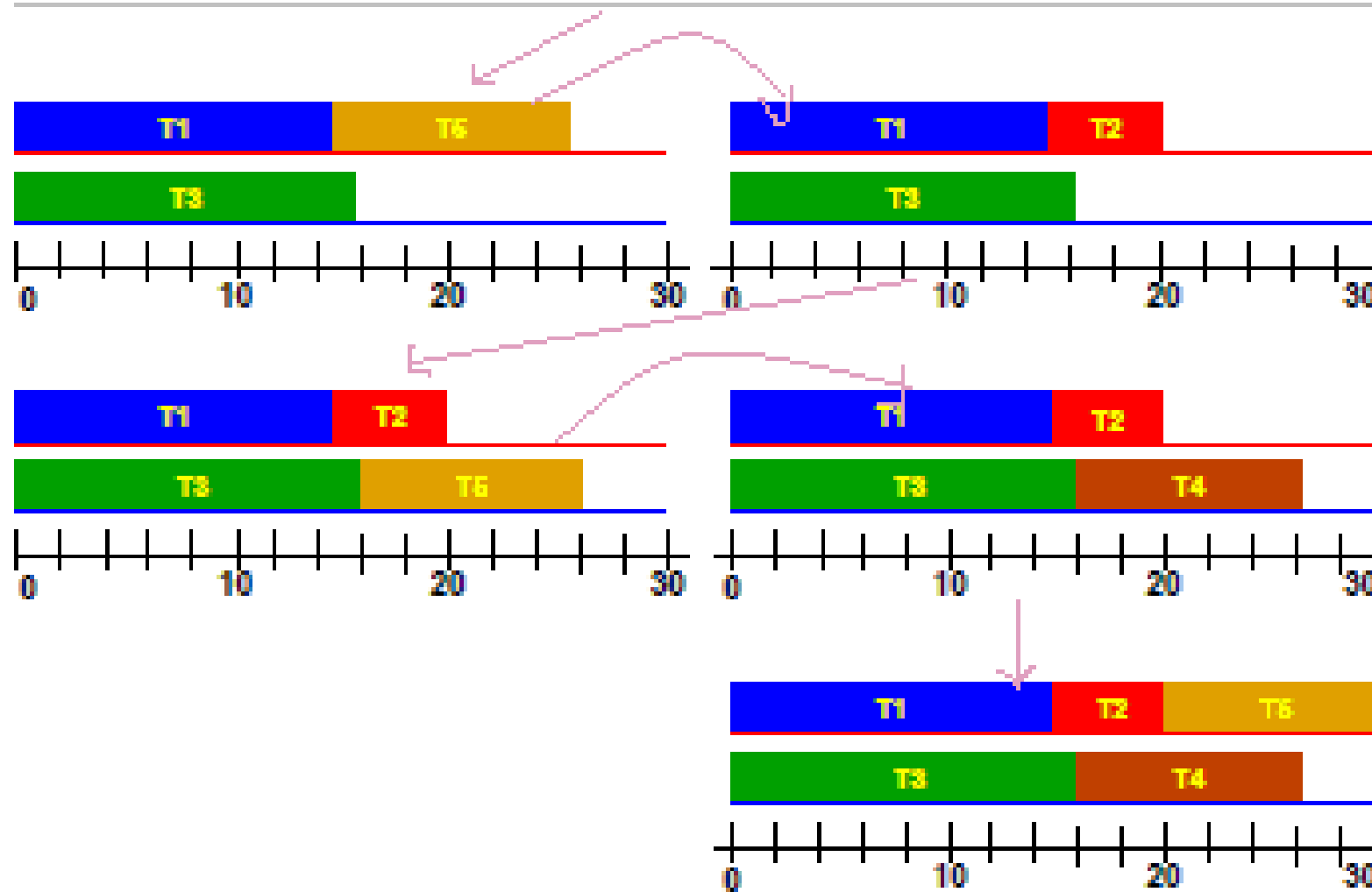
# Myopic Offline Scheduling algorithm/ Example

- ▶ That contains a schedule for T1. This node is strongly feasible – any of the other tasks can be feasibly scheduled given the position that T1 occupies in this schedule.
- ▶ Next, we pick T3 and schedule it to form a level – 2 mode. This is also strongly feasible. Then we generate a level–3 schedule, which involves augmenting the previous schedule with T5.
- ▶ Unfortunately, this is not strongly feasible.
- ▶ In particular, it would be impossible to augment this schedule with T2.

# Myopic Offline Scheduling algorithm/ Example

- ▶ So, we backtrack to the level-2 (i.e. the parent node). We pick T2 rather than T5 (the next task in order of release time) and schedule it.
- ▶ This results in a strongly feasible schedule.
- ▶ Next, we form a level-5 node by adding T5 to the schedule.
- ▶ This is not strongly feasible – T4 can not be added to it.
- ▶ So, we abandon this node, return to the parent (level-4) node.
- ▶ Generate a schedule by adding T4. This is strongly feasible.
- ▶ Then adding T5.

# Myopic Offline Scheduling algorithm





# Myopic Offline Scheduling algorithm

- ▶ The running time of the algorithm depends on  $K$  and  $H$ .
- ▶  $K$  bounds the number of tasks that the algorithm considers in determining the strong feasibility of a node.
- ▶ **If  $K$  is too small**, it is possible for us to declare a node to be strongly feasible and develop it further, only to find that none of its descendants is strongly feasible.

# Myopic Offline Scheduling algorithm

- ▶ If  $K$  is too large, we will spend a great deal of time (especially in the levels of the tree close to the root) checking the strong feasibility of nodes.
- ▶ In general, the tighter the constraints, the greater must be the value of  $K$ .
- ▶ In other words, if the task laxities are low or if many tasks use resources in addition to the processor,  $k$  must be large.
- ▶ It has been suggested,  $K = 13$  is the largest value ever required.

# Myopic Offline Scheduling algorithm

- ▶  $H$  is a weighted sum of the deadline and **earliest start time** is perhaps the most promising function.
- ▶ Homework: Resolve the example with  $H(i) = D_i$  and see if it runs faster for that function.