

# 1's complement and 2's complement

- We would explain Binary Arithmetic operations before explaining 1's and 2's complement, there are four arithmetic operations as in a decimal system:

## 1- Addition

The 4 basic rules for adding binary digits (bits) are as follows:

$$0 + 0 = 0$$

$$0 + 1 = 1$$

$$1 + 0 = 1$$

$$1 + 1 = 0 \text{ with carry } 1$$

$$\text{Example: } 11001 + 10011 = 101100_2$$

## 2- Subtraction

The four basic rules for subtracting bits as follows:

$$0 - 0 = 0$$

$$1 - 0 = 1$$

$$1 - 1 = 0$$

$$0 - 1 = 10 - 1 = 1 \text{ with borrow of } 1$$

$$\text{Example: } 11101 - 10110 = 00111_2$$

## 3- Multiplication

The four basic rules for multiplying bits are as follows:

$$0 * 0 = 0$$

$$0 * 1 = 0$$

$$1 * 0 = 0$$

$$1 * 1 = 1$$

$$\text{Example: } 111 * 101 = 100011_2$$

## 4- Binary division

The rules for division by binary bits is as follows:

$$0 \div 1 = 0$$

$$1 \div 1 = 1 \quad \text{where division by zero is not permitted}$$

Example:  $110 \div 10 = 10_2$

■ 1's complement:

- Subtraction of a number from another one can be achieved by adding the 1's complement of the subtrahend to the minuend.
- A form of signed binary in which negative numbers are created by complementing all bits.
- Subtraction of binary numbers using the 1's complement method can be achieved by addition.
- 1- Subtraction of smaller number from larger number as the following steps:

**Step1:** The 1's complement of a binary number can be obtained by changing all 1s to 0s and all 0s to 1s on the (subtrahend).

**Step2:** Add the result from step 1 to the larger number (minuend), the result is positive number.

**Step3:** Carry will be generated after the addition which is called End-round carry.

**Step4:** Remove the carry and add it to the result. This carry is called end-around-carry.

Example:

subtract  $(1010)_2$  from  $(1111)_2$  using 1's complement

**Subtract  $(1010)_2$  from  $(1111)_2$**

**Direct Subtraction**

$$\begin{array}{r} 1111 \\ - 1010 \\ \hline 0101 \end{array}$$

**1's complement method**

1's complement  $\rightarrow$   $\begin{array}{r} 1111 \\ + 0101 \\ \hline 10100 \end{array}$

Carry  $\rightarrow$   $\begin{array}{r} 10100 \\ + 1 \\ \hline 0101 \end{array}$

- 2- Subtraction a larger number from the smaller number as the following steps:

**Step1:** Determine the 1's complement of the larger number ( Subtrahend).

**Step2:** Add 1's complement to the smaller number (minuend).

**Step3:** We will get No carry.

**Step4:** The result will be negative number, to get the result in true form, take the 1's complement of the result and put assign -ve sign to the answer.

**Example:**

*subtract  $(11001)_2$  from  $(10101)_2$  using 1's complement*

$$\begin{array}{r}
 10101 \\
 - 11001 \\
 \hline
 \end{array}
 \xrightarrow{\text{1's complement}}
 \begin{array}{r}
 10101 \\
 - 00110 \\
 \hline
 11011
 \end{array}$$

No Carry ←

↓  
1's complement

Result → - 00100

### ■ 2's complement:

The subtraction can be done using 2's complement.

- 1- Subtraction of smaller number from larger number as the following steps:

**Step1:** determine the 2's complement of smaller number ( subtrahend).

**Step2:** Add 2's complement to the larger number ( minuend ).

**Step3:** discard the carry generated. Always a carry is generated in this case.

**Example:**

subtract  $(1010)_2$  from  $(1111)_2$  using 2's complement

**Subtract  $(1010)_2$  from  $(1111)_2$**

Direct Subtraction		2's complement method
$\begin{array}{r} 1111 \\ - 1010 \\ \hline 0101 \end{array}$		$\begin{array}{r} 1111 \\ + \\ \hline 0110 \\ \hline 10101 \end{array}$
	2's complement $\rightarrow$	
	Carry $\rightarrow$	

- 2- Subtraction a larger number from the smaller number as the following steps:

**Step1:** Specify the 2's complement of larger number ( subtrahend).

**Step2:** Add 2's complement to the smaller number ( minuend ).

**Step3:** To get the answer in the true form, take 2's complement and assign negative sign to the answer, no carry is generated in this method.

**Example:**

*subtract  $(1101)_2$  from  $(11011)_2$  using 2's complement*

$$\begin{array}{r}
 1101 \\
 11011 \\
 \hline
 \end{array}
 \begin{array}{l}
 \xrightarrow{1's} 01101 \\
 - \xrightarrow{1's} 00101 + \\
 \hline
 10010 \leftarrow \text{No Carry}
 \end{array}$$

$\downarrow$   
 taking 2's complement  $\rightarrow 01110$

### ■ 9's complement:

- 9's complement of a decimal number can be obtained by subtracting it from 9.

Example:

Find the 9's complement of the following numbers: 6, 212, 7905

$$9 - 7 = 3$$

$$999 - 212 = 787$$

$$9999 - 7905 = 2094$$

- 1- Subtraction of smaller number from larger number as the following steps:

**Step1:** produce 9's complement of subtrahend.

**Step2:** Adding the result of step 1 with Minuend.

**Step3:** There will be carry that can be added to the result, this is called (End Around Carry).

Example:

$$\begin{array}{r}
 83 \\
 - 29 \\
 \hline
 54
 \end{array}
 \quad
 \begin{array}{c}
 \xrightarrow{\hspace{1cm}} \\
 \xrightarrow{\hspace{1cm}}
 \end{array}
 \begin{array}{r}
 83 \\
 70 \\
 \hline
 153 + \xrightarrow{\hspace{1cm}} 54
 \end{array}$$

----- 9's complement
-----

54

 $\begin{array}{c} \text{1} \\ \text{5} \\ \text{3} \end{array} + \xrightarrow{\hspace{1cm}} 54$

..

 $\begin{array}{c} \text{1} \\ \text{5} \\ \text{3} \end{array} + \xrightarrow{\hspace{1cm}} 54$

- 2- Subtraction a larger number from the smaller number as the following steps:

**Step1:** produce 9's complement of Subtrahend.

**Step2:** Add the produced result from Step 1 to Minuend.

**Step3:** There is no carry in the produced result, so change the result to 9's complement and putting -Ve sign.

**Example:**

Perform the following subtraction using 9's complement

$$\begin{array}{r}
 56 \\
 - 87 \\
 \hline
 68
 \end{array}
 \quad
 \begin{array}{c}
 \xrightarrow{\hspace{1cm}} \\
 \xrightarrow{\hspace{1cm}}
 \end{array}
 \begin{array}{r}
 56 \\
 12 \\
 \hline
 68 \text{ No carry}
 \end{array}$$

Produce 9's complement with -ve sign  
 The result is  $99 - 68 = -31$

■ 10's complement:

- 10's complement of a decimal number can be obtained by obtaining 9's Plus 1.

Example:

Find the 10's complement of the following numbers: 26,360

$$99 - 26 = 73 \quad 73 + 1 = 74 \text{ is the } 10's \text{ complement of } 26$$

$$999 - 360 = 639 \quad 639 + 1 = 640 \text{ is the } 10's \text{ complement of } 360$$

- 1- Subtraction using 10's complement method of smaller number from larger number.

Example:

$$\begin{array}{r} 83 \\ - 25 \\ \hline \end{array} \quad \Longrightarrow \quad \begin{array}{r} 83 \\ + 75 \\ \hline \end{array} \quad \longleftarrow \text{10's complement}$$

carry discard  $\rightarrow 1 \quad 58$

Here the carry is generated, then we discard it, the remaining value is true answer a positive number (+ve).



- 2- Subtraction using 10's complement method of larger number from smaller number.

Example:

$$\begin{array}{r}
 37 \\
 - 69 \\
 \hline
 \end{array}
 \quad \longrightarrow \quad
 \begin{array}{r}
 37 \\
 31 + \\
 \hline
 68
 \end{array}
 \quad \longleftarrow \quad \text{10's complement. of 69}$$

**Here there is no carry, so taking 10's complement of the result to obtain the final result and adding a -ve sign**

**The answer is -32**