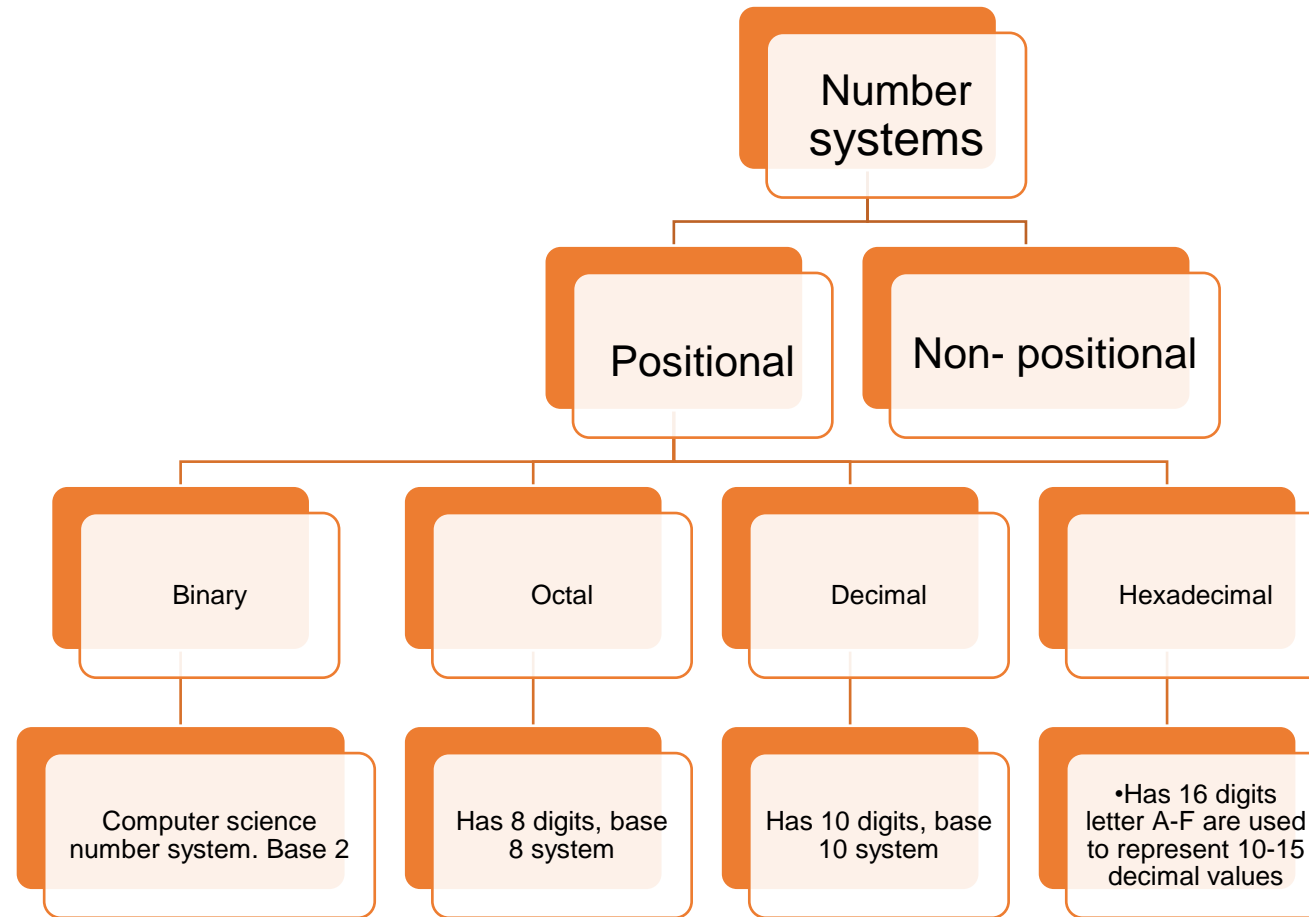


Logical Design

Lecture 2 :Number Systems

Dr Zaid Jafer Fadil

Number Systems



Conversion From Other Bases to Decimal Number System

Binary to Decimal

A number with base 2 is converted into number with base 10. Each binary digit here is multiplied by decreasing power of 2. Let us see one example:

Example: Convert $(11011)_2$ to decimal number.

We need to multiply each binary digit with the decreasing power of 2. That is;

$$1 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 1 \times 2^0$$

$$= 16 + 8 + 0 + 2 + 1 = 27$$

$$\text{Therefore, } (11011)_2 = (27)_{10}$$

Octal to Decimal Conversion

A number with base 8 is converted into number with base 10. Each digit of octal number here is multiplied by decreasing power of 8.

Example: Convert 121_8 into the equivalent decimal number.

Solution: Given $(121)_8$ is an octal number

Here, we have to multiply each octal digit with the decreasing power of 8, such as;

$$1 \times 8^2 + 2 \times 8^1 + 1 \times 8^0$$

$$= 64 + 16 + 1$$

$$= 81$$

Hexadecimal to Decimal Conversion

Each digit of hex number here is multiplied by decreasing power of 16.

Example: Convert 12_{16} into a decimal number.

Solution: Given 12_{16}

Multiply each digit with decreasing power of 16 to obtain an equivalent decimal number.

$$1 \times 16^1 + 2 \times 16^0$$

$$= 16 + 2$$

$$= 18$$

Number System Relationship

HEXADECIMAL	DECIMAL	OCTAL	BINARY
0	0	0	0000
1	1	1	0001
2	2	2	0010
3	3	3	0011
4	4	4	0100
5	5	5	0101
6	6	6	0110
7	7	7	0111
8	8	10	1000
9	9	11	1001
A	10	12	1010
B	11	13	1011
C	12	14	1100
D	13	15	1101
E	14	16	1110
F	15	17	1111