

Maximum : **0** 1 1 1 1 1 1 1 = +127

- For *-ve* number

Minimum : **1** 0 0 0 0 0 0 0 = -128

Maximum : **1** 1 1 1 1 1 1 1 = -1

Range ==> -128 —> +127

BY Dr. Faris

Binary Coded Decimal (BCD).

- A code used to represent each decimal digit of a number by a 4-Bit Binary Value.
- Valid Digits (combinations) for 0 to 9 are 0000 to 1001.
- Invalid Digits (combinations) (10 – 15).
- The binary codes 1010 to 1111 are invalid.
- Called an 8421 Code due to the decimal weight of each bit position.
- The following table represents a conversion of decimal number to BCD.

Decimal Digit	BCD 8 4 2 1
0	0 0 0 0
1	0 0 0 1
2	0 0 1 0
3	0 0 1 1
4	0 1 0 0
5	0 1 0 1
6	0 1 1 0
7	0 1 1 1
8	1 0 0 0
9	1 0 0 1

- One decimal digit + one decimal digit
- If the result is "1" decimal digit (≤ 9), then it is a simple binary addition.

Example:

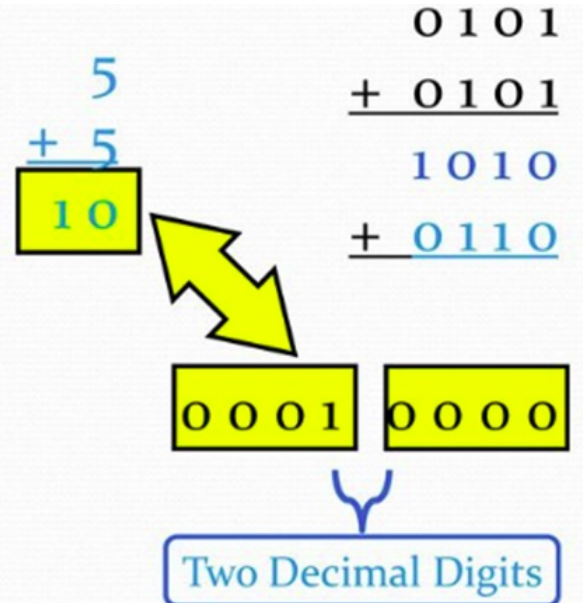
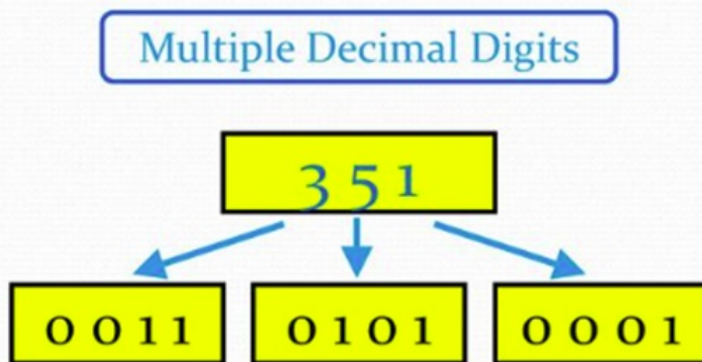
$$\begin{array}{r} 5 \\ + 3 \\ \hline 8 \end{array} \longleftrightarrow \begin{array}{r} 0101 \\ + 0011 \\ \hline 1000 \end{array}$$

- If the result is two decimal digits (≥ 10), then binary addition gives invalid combinations

Example:

$$\begin{array}{r} 5 \\ + 5 \\ \hline 10 \end{array} \longleftrightarrow \begin{array}{r} 0001 \\ 0000 \end{array} \longleftrightarrow \begin{array}{r} 0101 \\ + 0101 \\ \hline 1010 \end{array}$$

- If the binary result is greater than 9, correct the result by adding 6



Example:

Convert each of the following decimal numbers to BCD

A- 45

B- 2693

$$\text{A- } 45 = \overbrace{0100}^4 \overbrace{0101}^5$$

$$\text{B- } 2693 = \overbrace{0010}^2 \overbrace{0110}^6 \overbrace{1001}^9 \overbrace{0011}^3$$

Gray Code.

- The Gray Code is non weighted code in which each number differs from previous number by a single bit.
- Different than Binary Code.
- Binary: $b_3b_2b_1b_0$, Gray: $g_3g_2g_1g_0$.
- Gray code bits can be defined as follows:

- $g3 = b3$
 $g2 = b3 \oplus b2$
 $g1 = b2 \oplus b1$
 $g0 = b1 \oplus b0$

Decimal	Binary	Gray code
0	0000	0000
1	0001	0001
2	0010	0011
3	0011	0010
4	0100	0110
5	0101	0111
6	0110	0101
7	0111	0100
8	1000	1100
9	1001	1101

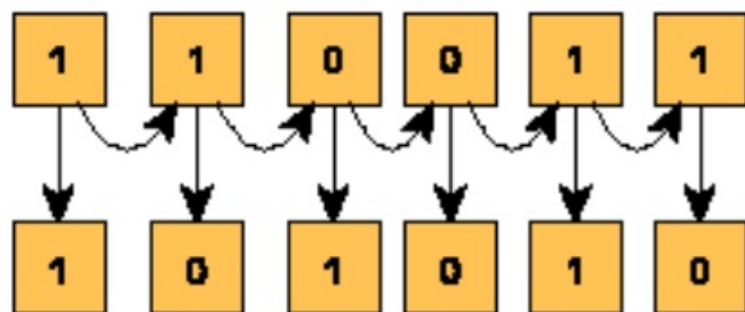
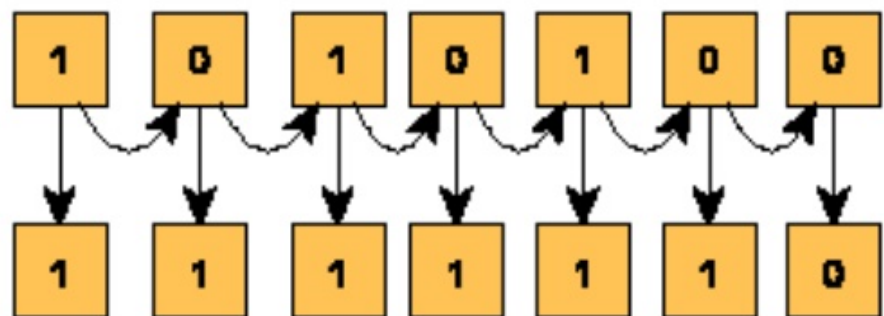
- Binary to Gray conversion.

- 1— The MSB in the Gray code is same as the corresponding bit in the binary number.
- 2— Going from left to right, add each adjacent pair of binary bit to get next Gray code bit and discard carry.

11 or 00 \longrightarrow **0 (similar put 0)**

01 or 10 \longrightarrow **1 (different put 1)**

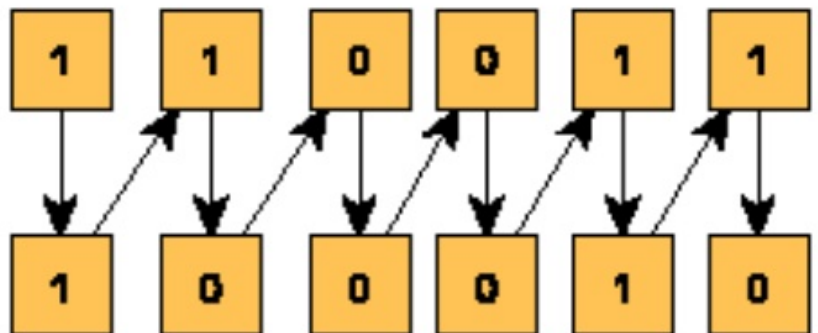
Examples:



- **Gray to Binary conversion.**

- 1– The MSB is the binary code is same as corresponding digit in the Gray code.
- 2– Add each binary digit generated to the Gray digit in the next adjacent position and discard carry.

Example:



Excess code 3.

- A BCD Code formed by adding 3 (0011) to its true 4-bit binary value.
- Excess-3 is a self-complementing code:
- A negative code equivalent can be found by inverting the binary bits of the positive code.
- Inverting the bits of the Excess-3 digit yields 9's Complement of the decimal equivalent.

Example:

- $3 = 0011 + 0011 = 0110 = 6$ in E3
- $1 = 0001 + 0011 = 0100 = 4$ in E3
- If we complement $1 = 1011$ in E3, this is the code for an 8.
- 9's complement of 1 = (9-1) 8 (self-complement).