

Example: Solve the I.V.P.

$$\frac{dy}{dx} = x - y, \quad y(0) = 1$$

By using Runge-Kutta4 method at the points $x = 0.1, 0.2, 0.3, 0.4$

```
% Runge-Kutta4 method to solve I.V.P.
```

```
clear;
clc;
a=0;
b=0.4;
n=4;
y0=1;
f=@(x,y) x-y;
h=(b-a)/n;
y=zeros(1,n+1);
x=zeros(1,n+1);
x(1)=a;
y(1)=y0;
for k=1:n
    x(k+1)=x(k)+h;
    k1=h*f(x(k),y(k));
    k2=h*f(x(k)+h/2,y(k)+k1/2);
    k3=h*f(x(k)+h/2,y(k)+k2/2);
    k4=h*f(x(k)+h,y(k)+k3);
    y(k+1)=y(k)+(k1+2*k2+2*k3+k4)/6;
end
disp('    x          y    ')
disp(' -----')
disp([x' y'])
```

x	y
-----	-----
0	1.0000
0.1000	0.9097
0.2000	0.8375
0.3000	0.7816
0.4000	0.7406