

في الحالة التي يكون فيها المدخل مساوي للخارج  
 For example: (أي ان قيم  $x$  هي نفس قيم  $y$ )  
 $f(x) = x$  ;  $f(0) = 0$  ,  $f(1) = 1$  and so on

### 3. Absolute Function

$$y = |x| = \begin{cases} -x & \text{if } x < 0 \\ x & \text{if } x \geq 0 \end{cases}$$

### 4. Integer Function

$$y = \llbracket x \rrbracket \quad \text{for example.}$$

$$y = f(3.1) = \llbracket 3.1 \rrbracket = 3$$

$$f(-1.6) = \llbracket -1.6 \rrbracket = -2$$

### 5. Odd and Even Functions

we say that  $f(x)$  is even function if:

$$f(-x) = f(x) \quad ; \quad \text{The opposite, it is odd}$$

Ex  $f(x) = \frac{x^2}{x^4 + 1}$

Solu  $f(-x) = \frac{(-x)^2}{(-x)^4 + 1} = \frac{x^2}{x^4 + 1} = f(x)$

$$\therefore f(-x) = f(x)$$

$f(x)$  is even function

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$$\underline{\text{Ex}} \quad f(x) = \frac{1}{x} \quad ; \quad f(-x) = -\frac{1}{x}$$

$$\therefore f(x) \neq f(-x)$$

$\therefore f(x)$  is not even ;  $f(x)$  is odd function

There are functions that are neither even and odd ; for example:-

$$f(x) = x^2 - 3x + 5$$

1.  $f(-x) = (-x)^2 - 3(-x) + 5 = x^2 + 3x + 5 \neq f(x)$

2.  $-f(x) = -(x^2 - 3x + 5) = -x^2 + 3x - 5 \neq f(x)$

$\therefore f(x)$  is not odd and not even

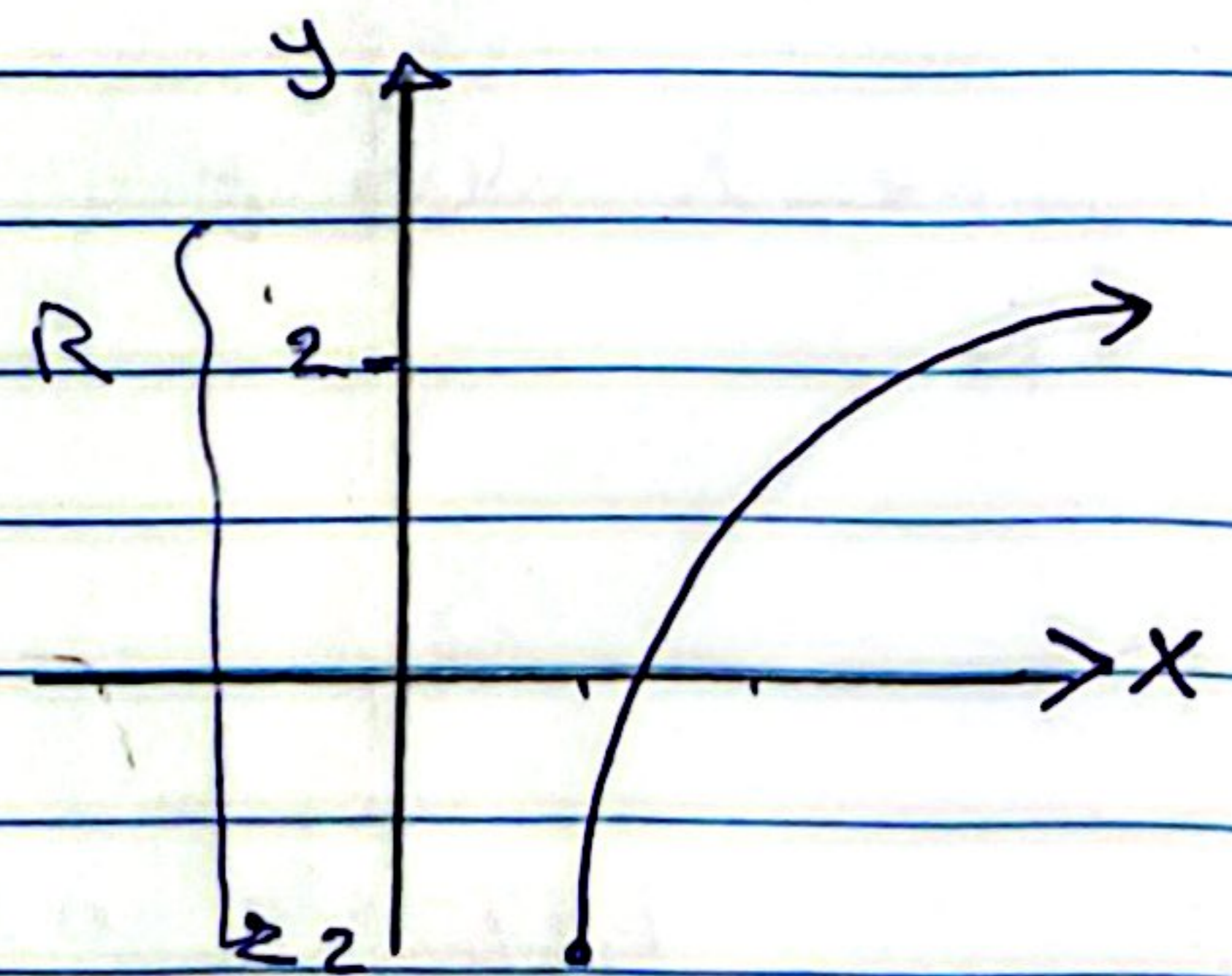
ايجاد المدى، القيمة العظمى والصغرى وكالاتي

Ex Find the range to :-

1.  
 $\text{Domain} = [-2, \infty)$

$$R = \{x : x \in \mathbb{R}\} = [-2, \infty)$$

or  $R = \infty > y \geq -2$

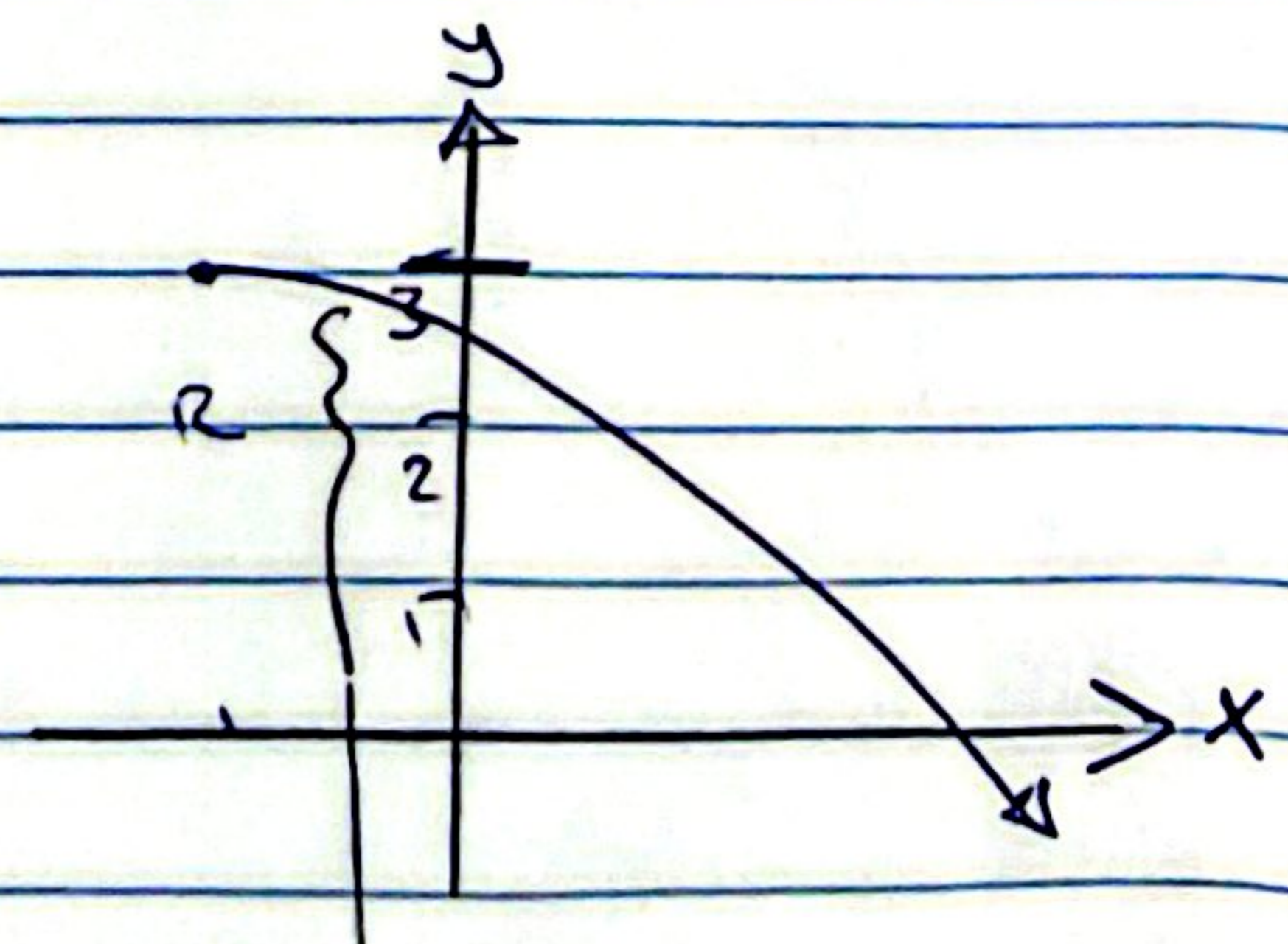


2.

$$\text{Domain} = (-\infty, 3]$$

$$R = \{x : x \in \mathbb{R}\} = (-\infty, 3]$$

or  $R = y \leq 3$

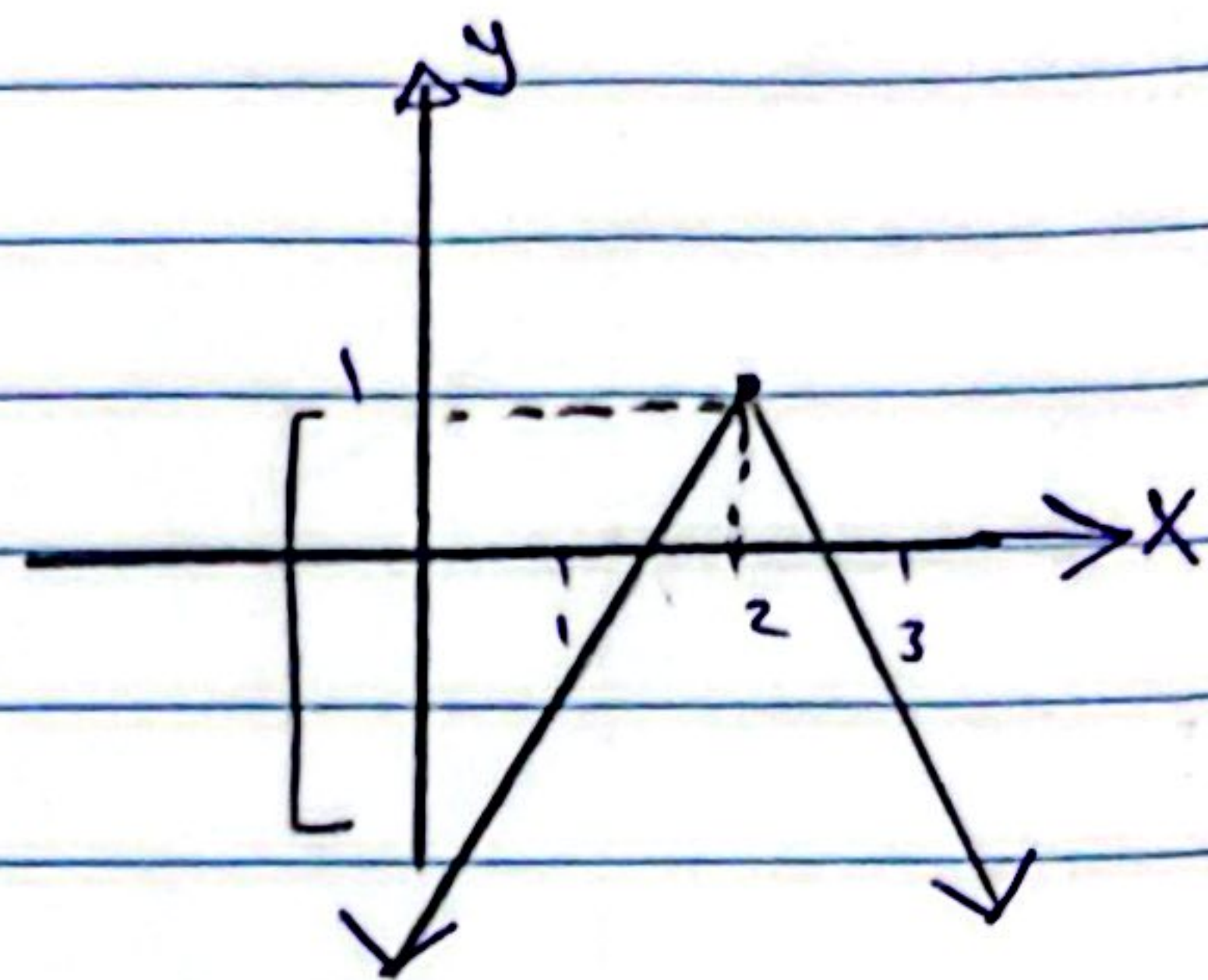


3.

$$D_{\text{subl}} = (-\infty, 1]$$

$$R = \{x : x \in \mathbb{R}\} = (-\infty, 1]$$

$$\text{or } R = y < 1$$

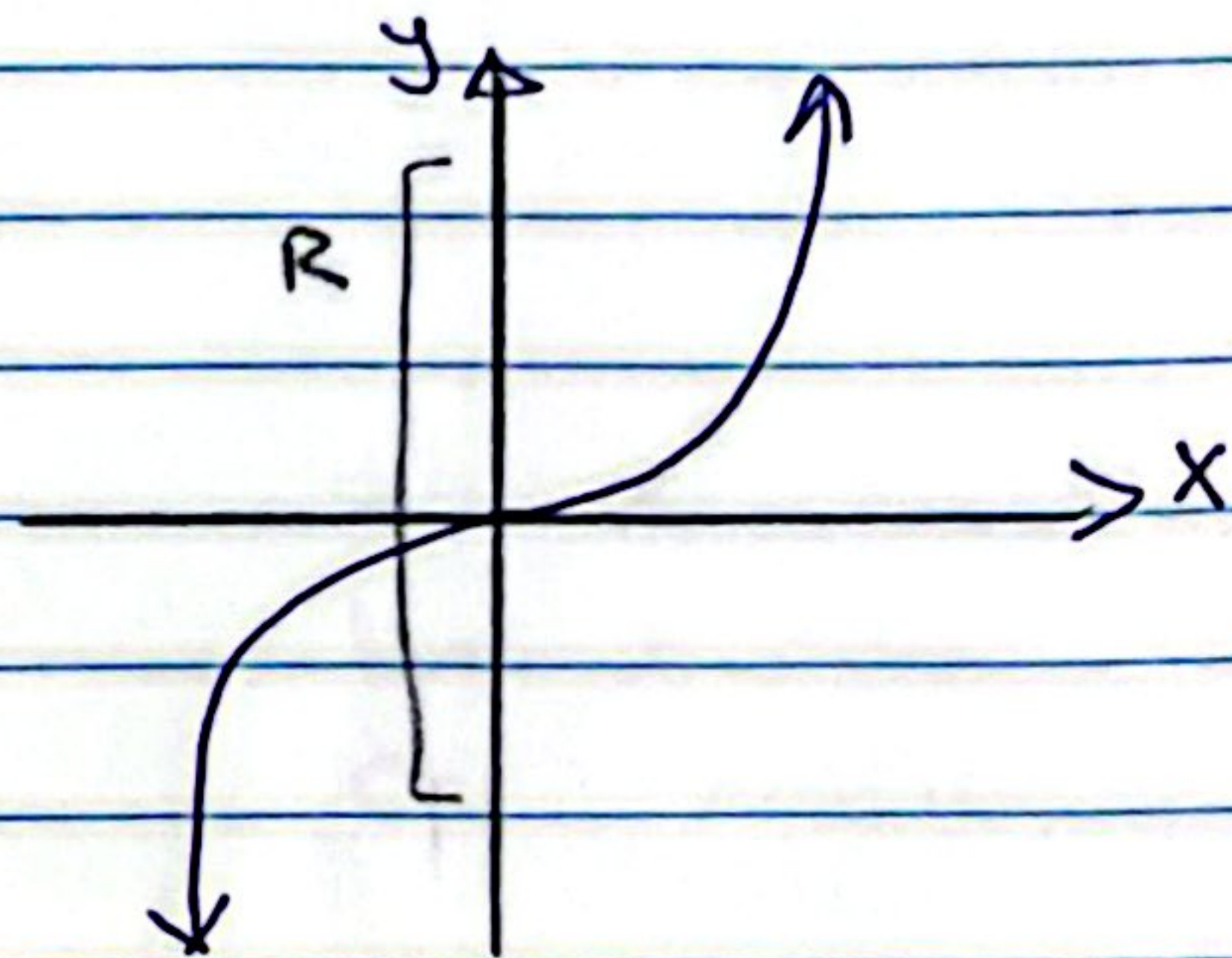


4.

$$D_{\text{subl}} = (-\infty, \infty)$$

$$R = \{x : x \in \mathbb{R}\} = (-\infty, \infty)$$

$$\text{or } y = \mathbb{R}$$



Ex Find the Range to: إيجاد المدى جبرياً

$$1. \quad y = \frac{x+1}{x-2} \quad ; \quad x \neq 2$$

$$D = \mathbb{R} \setminus \{2\}$$

Solyتبدل  $x$  بـ  $y$ 

$$xy - 2y = x + 1$$

$$xy - x = 2y + 1$$

$$x(y-1) = 2y+1$$

$$x = \frac{2y+1}{y-1}$$

$$; \quad y-1 \neq 0 \Rightarrow y \neq 1$$

$$R = \{y : y \in \mathbb{R} ; 1\}$$

المدى