

$$3. \lim_{x \rightarrow 1} \frac{x^2 + x - 2}{x^2 - x}$$

١. التعويض

$$\frac{1+1-2}{1-1} = \frac{0}{0}$$

٢. التبسيط

بذلك بالتجربة

$$= \lim_{x \rightarrow 1} \frac{(x+2)(x-1)}{x(x-1)}$$

$$= \lim_{x \rightarrow 1} \frac{x+2}{x}$$

$$= \frac{3}{1} = 3$$

$$4. \lim_{x \rightarrow 2} \frac{x^3 - 8}{x - 2}$$

Solu

$$\frac{8-8}{2-2} = \frac{0}{0}$$

لا يجوز

$$\therefore = \lim_{x \rightarrow 2} \frac{(x-2)(x^2+2x+4)}{(x-2)}$$

$$= \lim_{x \rightarrow 2} (x^2+2x+4)$$

$$= 2^2 + 2(2) + 4 = 12$$

$$5. \lim_{x \rightarrow -1} \frac{1}{x^2+2}$$

Solu

$$\lim_{x \rightarrow -1} \frac{1}{x^2+2} = \frac{1}{1+2} = \frac{1}{3}$$

So that the limit of the function $\lim_{x \rightarrow -1} \frac{1}{x^2+2}$ when x approaches -1 is $\frac{1}{3}$.

limits

To explain the limit of a function, we consider the following mathematical definition:

$$f: \mathbb{R} \rightarrow \mathbb{R}$$

Let have the function

$$f(x) = x^2 - 1 \quad ; x \in \mathbb{R}$$

We want to know what happens to the value of the function $f(x)$, when we give values for x that are very close to 2 on both sides that is, we give values of x are a little less than 2, a little more than 2, and so on.

This is what is meant by the expression "very close to 2" from both sides.

When we substitute values for x into the function, we get the result that the value of the function is very close to the number 3.

The closer the value of x is to the number 2, that is, we can say that the limit of the function.

$$f(x) = x^2 - 1 \quad \text{in the number 2 is 3}$$

$$\text{That is : } f(2) = 2^2 - 1 = 3$$

The limits are divided into three sections:

The limits are:

H.W. Find the Range and Domain to the Figures

1.

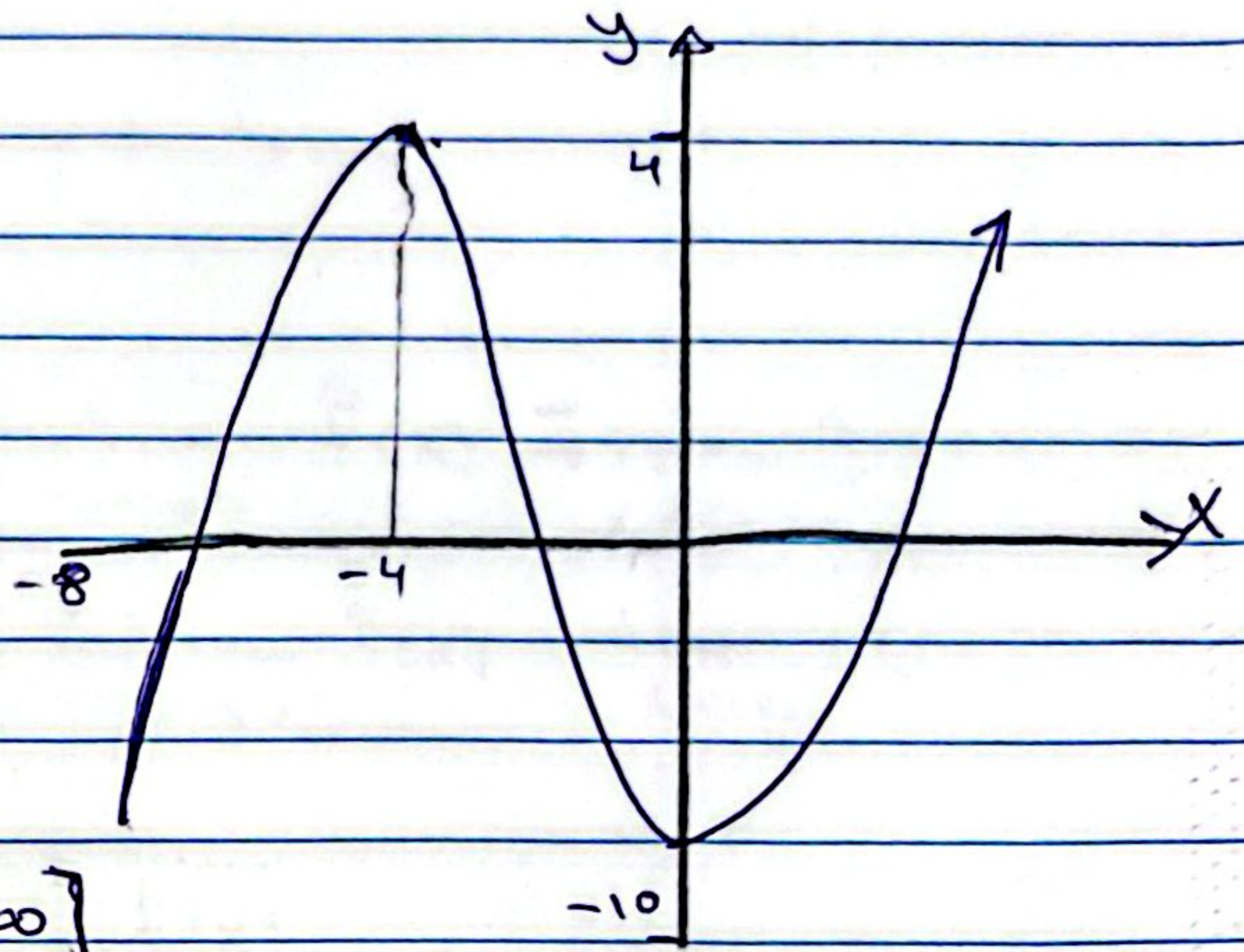
$$D = [-8, -4) \cup (-4, \infty)$$

or

$$D = \{x : x \in \mathbb{R}; x \geq -8\}$$

$$x \neq -4$$

$$R = \{y : y \in \mathbb{R}\} = [-10, \infty)$$



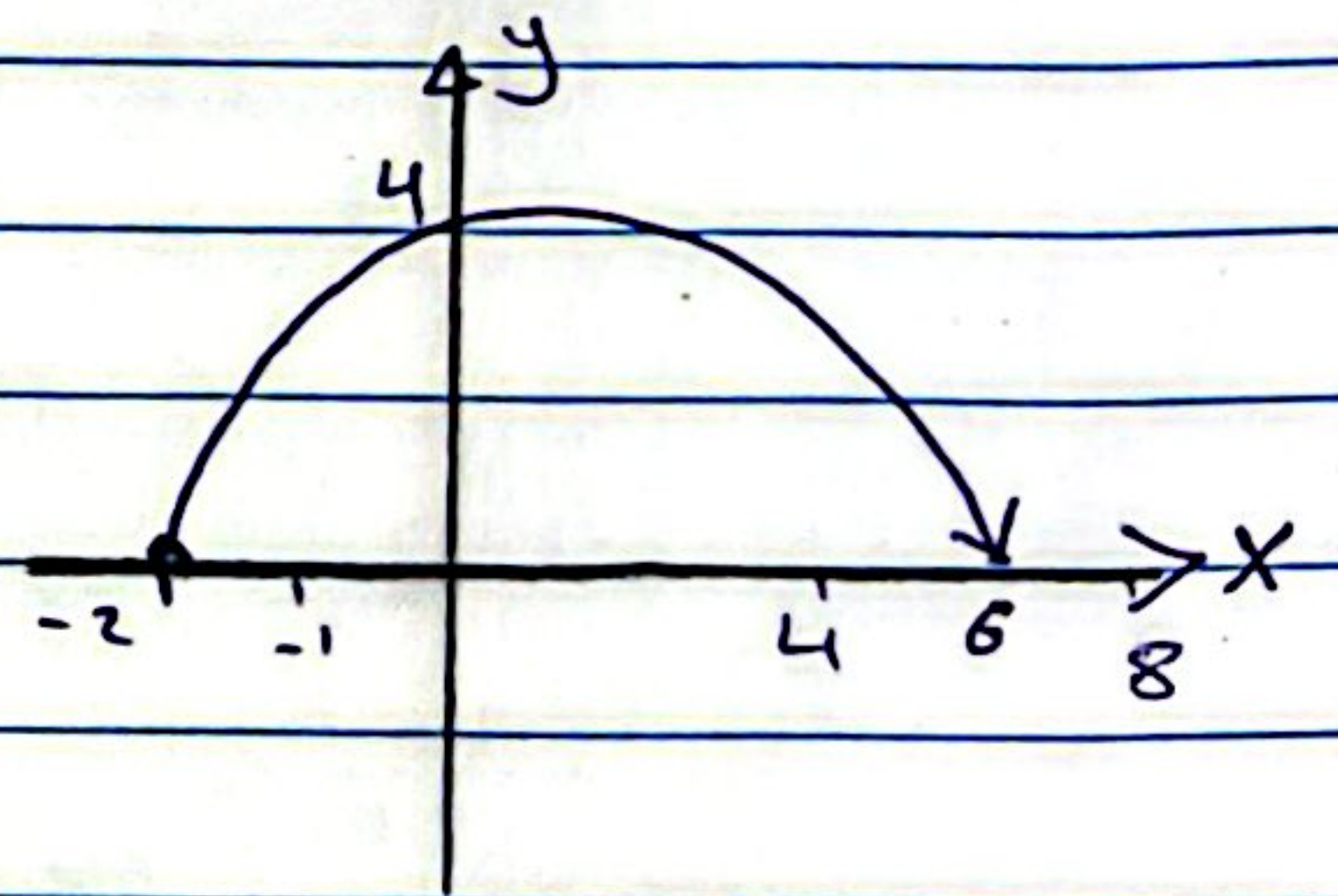
2.

$$D = \{x : x \in \mathbb{R}\} = [-2, 6]$$

or

$$D = [-2, 6)$$

$$R = \{y : y \in \mathbb{R}\} = [0, 4]$$



3.

$$D = \{x : x \in \mathbb{R}; x > -4; x \neq 2\}$$

$$\text{or } D = (-4, \infty) \cup (2, \infty)$$

$$R = \{y : y \in \mathbb{R}; y < -2; y = 6\}$$

$$\text{or } R = (-\infty, -2) \cup \{6\}$$

