

Analysis of Variance Table ANOVA

here's a complete, self-contained numerical example of a One-Way ANOVA, solved two ways: (A) direct/menu method (what you click in Minitab) and (B) commands/session method (Minitab Session commands). I'll show the dataset, full calculations (numbers), the ANOVA table, p-value, interpretation, and the exact Minitab commands you can paste into the Session window.

Example dataset

Three groups (3 treatments), 4 observations each:

Row	Group	Score
1	A	8
2	A	9
3	A	6
4	A	7
5	B	10
6	B	12
7	B	9
8	B	11
9	C	5
10	C	4
11	C	6
12	C	7

So Group A = {8, 9, 6, 7}; Group B = {10, 12, 9, 11}; Group C = {5, 4, 6, 7}.

Step 1 — summary statistics (computed)

- $n_1 = n_2 = n_3 = 4$, total $N = 12$
- Group means:

Analysis of Variance Table ANOVA
Mahmood81_tahr@uomosul ed.iq

- mean(A) = 7.5
- mean(B) = 10.5
- mean(C) = 5.5
- Grand mean $\bar{X}_{..} = 7.8333333333 (\approx 7.8333)$

Computed sums of squares:

- **SS_between (treatment) = $\sum n_j (\bar{X}_j - \bar{X}_{..})^2 = 50.6666666667$**
- **SS_within (error) = $\sum \sum (x_{ij} - \bar{X}_j)^2 = 15.0$**
- **SS_total = 65.6666666667 (SS_between + SS_within)**

Degrees of freedom:

- **DF_between = $k - 1 = 3 - 1 = 2$**
- **DF_within = $N - k = 12 - 3 = 9$**
- **DF_total = $N - 1 = 11$**

Mean squares:

- **MS_between = $SS_between / DF_between = 50.6666666667 / 2 = 25.3333333333$**
- **MS_within = $SS_within / DF_within = 15.0 / 9 = 1.6666666667$**

F statistic:

- **$F = MS_between / MS_within = 25.3333333333 / 1.6666666667 = 15.2$**

P-value (F with df1=2, df2=9):

- **$p \approx 0.00130$**

ANOVA table (numeric)

Source	DF	SS	MS	F	P
Between (Groups)	2	50.6667	25.3333	15.20	0.0013
Within (Error)	9	15.0000	1.6667		
Total	11	65.6667			

Interpretation: $p = 0.0013 < 0.05 \rightarrow$ **reject H_0** . There is strong evidence that **at least one group mean differs** from the others

Step 2 — Menu (direct) method in Minitab

1. **Enter the data** in the Worksheet:

- Put `Score` in column C1 (enter the 12 numeric values).
- Put `Group` in column C2 (enter categorical labels A, A, A, A, B, B, B, B, C, C, C, C).

Example layout:

- C1 = Score: 8,9,6,7,10,12,9,11,5,4,6,7
- C2 = Group: A,A,A,A,B,B,B,B,C,C,C,C

2. **Run One-Way ANOVA:**

- Menu: `Stat` \rightarrow `ANOVA` \rightarrow `One-Way` \rightarrow select **Response = Score (C1)** and **Factor = Group (C2)**.
- Click **OK**.
- (Optional) For multiple comparisons: in the One-Way dialog choose **Comparisons** \rightarrow select **Tukey** (or Bonferroni) to see pairwise tests.

3. **Read output:**

- The Session/Results window will show the ANOVA table (should match the numbers above) and any requested multiple comparisons.

Step 3 — Commands (Session commands) method in Minitab

```
MTB > OneWay;
```

```
SUBC> Response C2;
```

```
SUBC> Categorical C1;
```

```
SUBC> IType 0;
```

```
SUBC> end
```

```
MTB >
```

Regression Analysis

Let's cover Regression Analysis in Minitab using both methods:

1-Direct Method (Menus / Dialogs)

2-Indirect Method (Session Commands)

I'll use an easy example with numbers, then show both ways.

Example Dataset

We want to predict **Sales (Y)** from **Advertising Budget (X)**.

Row	Advertising (X)	Sales (Y)
1	10	25
2	20	40
3	30	45
4	40	60
5	50	65

```
MTB > Fitline C2 C3;  
SUBC> Confidence 95.0.  
MTB > Fitline 'y' 'x';  
SUBC> Confidence 95.0.  
MTB >
```

Regression Analysis: y versus x

Analysis of Variance Table ANOVA
 Mahmood81_tahr@uomosul ed.iq

The regression equation is

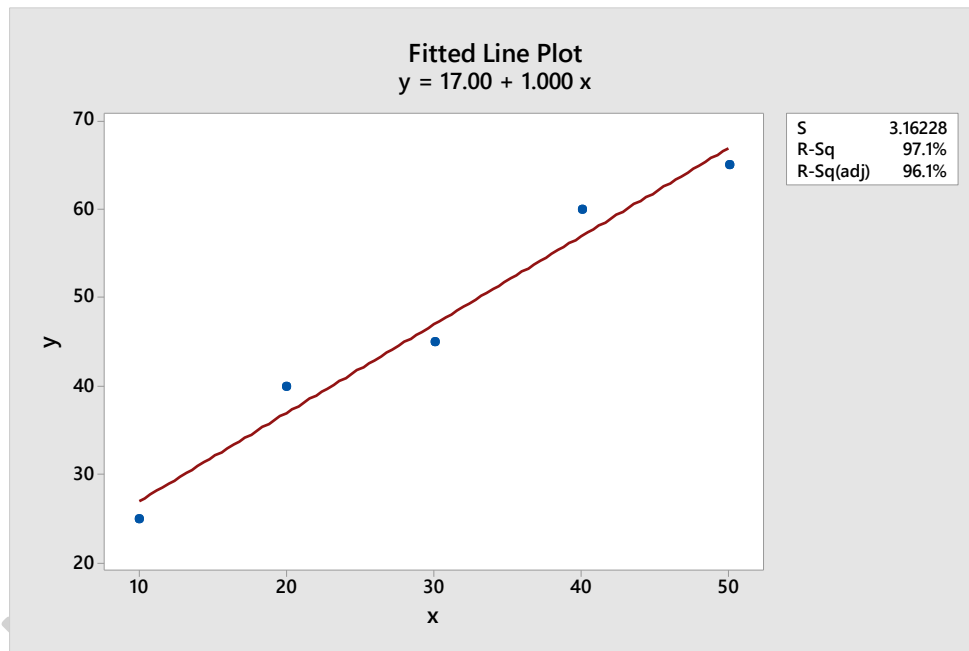
$$y = 17.00 + 1.000 x$$

Model Summary

S	R-sq	R-sq(adj)
3.16228	97.09%	96.12%

Analysis of Variance

Source	DF	SS	MS	F	P
Regression	1	1000	1000	100.00	0.002
Error	3	30	10		
Total	4	1030			



Summary

- **Direct Method (Menu):** Use Stat → Regression → Fit Regression Model → select Y and X → OK.
- **Indirect Method (Command):** Use REGRESS C2 1 C1. in Session Window.
- Both methods produce the **same regression equation, ANOVA table, coefficients, and model diagnostics.**