

Max operation

Let $A = (a_{ij})$ and $B = (b_{ij})$ be any two $m \times n$ fuzzy matrices; define $\text{Max}(A, B) = (\text{Max}(a_{ij}, b_{ij}))$, $a_{ij} \in A$ and $(b_{ij} \in B, 1 \leq i \leq m \text{ and } 1 \leq j \leq n$. Then $\text{Max}(A, B)$ is a fuzzy matrix. This operation will be known as Max operation.

$$\max(A, B) = \max\{\mu_A(x_i, y_j), \mu_B(x_i, y_j)\}, \\ \mu_A(x_i, y_j) \in A, \mu_B(x_i, y_j) \in B, 1 \leq i \leq m, 1 \leq j \leq n$$

EX:

Let A,B be any two 3×4 fuzzy matrices find $\text{Max}(A, B)$

$$A = \begin{bmatrix} 0.8 & 1 & 0 & 0.3 \\ 0.3 & 0.2 & 0.4 & 1 \\ 0.1 & 0 & 0.7 & 0.8 \end{bmatrix} \quad B = \begin{bmatrix} 0.9 & 0.8 & 0.7 & 0 \\ 0.1 & 1 & 0 & 0.3 \\ 0.2 & 0.5 & 0.5 & 0.8 \end{bmatrix}, \max(A, B) = \begin{bmatrix} 0.9 & 1 & 0.7 & 0.3 \\ 0.3 & 1 & 0.4 & 1 \\ 0.2 & 0.5 & 0.7 & 0.8 \end{bmatrix}$$

clearly $\text{Max}(A, B)$ is again a fuzzy matrix as every entry given by $\text{Max}(A, B)$ belongs to the interval $[0, 1]$.

It is interesting to note $\text{Max}(A, A) = A$ and $\text{Max}((0), A) = A$ where (0) is the zero matrix of the same order as that of A .